

SCIENTIFIC REPORTS



OPEN

Initial pseudo-steady state & asymptotic KPZ universality in semiconductor on polymer deposition

Renan A. L. Almeida¹, Sukarno O. Ferreira², Isnard Ferraz² & Tiago J. Oliveira²

The Kardar-Parisi-Zhang (KPZ) class is a paradigmatic example of universality in nonequilibrium phenomena, but clear experimental evidences of asymptotic 2D-KPZ statistics are still very rare, and far less understanding stems from its short-time behavior. We tackle such issues by analyzing surface fluctuations of CdTe films deposited on polymeric substrates, based on a huge spatio-temporal surface sampling acquired through atomic force microscopy. A *pseudo*-steady state (where average surface roughness and spatial correlations stay constant in time) is observed at initial times, persisting up to deposition of $\sim 10^4$ monolayers. This state results from a fine balance between roughening and smoothening, as supported by a phenomenological growth model. KPZ statistics arises at long times, thoroughly verified by universal exponents, spatial covariance and several distributions. Recent theoretical generalizations of the Family-Vicsek scaling and the emergence of log-normal distributions during interface growth are experimentally confirmed. These results confirm that high vacuum vapor deposition of CdTe constitutes a genuine 2D-KPZ system, and expand our knowledge about possible substrate-induced short-time behaviors.

The Kardar-Parisi-Zhang (KPZ) equation¹

$$\partial_t h = \nu \nabla^2 h + \frac{\lambda}{2} (\nabla h)^2 + \sqrt{D} \eta(\mathbf{x}, t), \quad (1)$$

originally describes interface motion under conditions of no bulk conservation and exponentially fast relaxation². The height field $h(\mathbf{x}, t)$ is measured from a d_s -dimensional substrate at location \mathbf{x} , with $\mathbf{x} \in \mathbb{R}^{d_s}$ at time $t \geq 0$. ν , λ and D are phenomenological parameters, physically representing the surface tension, the excess of velocity in the growth, and the amplitude of a space-time white noise η , respectively.

Although posed 30 years ago, outstanding advances on the understanding of the KPZ class have been made quite recently. Following seminal works on multiple-meaning stochastic models^{3,4}, long-awaited analytical solutions^{2,5}, experiments^{6,7} and numerical simulations⁷⁻⁹ came out to confirm that *asymptotic* 1D-KPZ height distributions (HDs) are related to statistics of the largest eigenvalues of random matrices¹⁰, while spatial covariances are dictated by the *time*-correlation of Airy processes¹¹. Noteworthy, both HDs and covariances exhibit sensibility to initial conditions (ICs)^{4,11}, splitting the KPZ class into subclasses according to the ICs. This unanticipated feature was recently observed also in models for nonlinear molecular beam epitaxy class¹². Similar scenario has been found for the 2D-KPZ case, based on numerical simulations¹³⁻¹⁵, although no analytical result is known for 2D-KPZ HDs and covariances and the existing theoretical approaches^{16,17} for the scaling exponents disagree with numerical outcomes. In such arid landscape, the rare reliable experimental evidences of 2D-KPZ universality¹⁸⁻²¹ turns to be precious achievements.

The short-time roughening of systems exhibiting asymptotic KPZ scaling is also rich in behavior. For example, a transient scaling in the Edwards-Wilkinson²² (EW) class, might appear whenever λ is “small” when compared to ν and D . On the other hand, if these parameters satisfy the condition $D \gg (\nu, \lambda)$, then a transient Random

¹Tokyo Institute of Technology, Department of Physics, 2-12-1 Ookayama, Meguro-ku, Tokyo, 152-8551, Japan.

²Departamento de Física, Universidade Federal de Viçosa, 36570-900, Viçosa, Minas Gerais, Brazil. Correspondence and requests for materials should be addressed to R.A.L.A. (email: lisboa.r.aa@m.titech.ac.jp) or T.J.O. (email: tiago@ufv.br)

Deposition (RD) scaling might take place. In both cases, a crossover to KPZ dynamics occurs at a characteristic time t_c . The EW-KPZ and RD-KPZ crossovers were intensively studied in competitive growth models^{23–25}, but are also related to the edge statistics of fermionic lattices at high-temperatures²⁶ and to synchronization problems in parallel computation²⁵. Besides a recent observation of RD-KPZ crossover in CdTe/Si(100) films deposited at $T = 200^\circ\text{C}$ ²¹, experimental studies showing crossovers to asymptotic KPZ scaling are mostly lacking, even though should be quite expected.

In this contribution, we show experimentally that a new type of short-time regime, differing from EW and RD, may take place during the growth of a semiconductor film on a polymeric substrate. Such system has a very important technological application in the fabrication of flexible solar cells²⁷. By analyzing surface fluctuations of CdTe films deposited on polyimide (Kapton) substrates, we reveal that the observed transient regime is characterized by Gaussian statistics, a constant roughness in time and *no* spreading of correlations through the system. Since these last characteristics are hallmarks of “saturated” interfaces, we will refer to that regime as a *pseudo*-steady state (PSS). After a long characteristic time t_c , corresponding to the deposition of $\sim 10^4$ monolayers of CdTe, correlations and height fluctuations start developing, yielding an asymptotic growth in the KPZ class. We show in fine experimental details properties of 2D-KPZ universality, by independently measuring several scaling exponents, universal distributions related to the height, roughness and extremal height fluctuations, as well as the rescaled spatial covariance. Experimental evidence of log-normal distributions in surface growth dynamics is also given.

Experimental Methods

We performed the experiment growing CdTe films onto polymeric substrates (Kapton, Dupont) by hot wall deposition technique in high-vacuum ($\sim 10^{-7}$ Torr). This growth technique has been chosen for its simplicity and for being demonstrated to yield high quality CdTe films with properties similar to films produced by molecular beam epitaxy^{28,29}. Substrate temperature was set to $T = 150^\circ\text{C}$, and source temperature to 510°C , yielding a growth rate $F = 14.0(3)$ nm/min. Different films were grown for several times varying from 7.5 min to 5760 min. Before the deposition, substrates were annealed (at $T = 150^\circ\text{C}$) inside the growth chamber for 15 min in order to release weakly bounded impurities and guarantee thermal homogeneity since the beginning of the deposition process. For each time a completely independent film was grown and its morphology was characterized by atomic force microscopy, using an NTEGRA-Prima SPM (NT-MDT). We collected about $\sim 10^7$ spatial points in total, in up to 10 different scanned regions for each film (time). Experimental data were analyzed by our own computational algorithms. The results were checked to be statistically independent of the AFM tip, lateral scan size (L) and operational mode (contact or tapping). In the following we show data from images taken at $L = 10\ \mu\text{m}$, with 512×512 pixels and contact mode. X-ray diffraction, with a D8-Discover diffractometer (BRUKER), was used to characterize the crystalline structure of the grown films.

Results and Discussions

Pseudo-steady state crossover to KPZ. *Experiments.* Surface morphologies of grown samples can be visually distinguished in two sets [see Fig. 1]. For times shorter than ≈ 300 min, the surface is constituted by a plethora of rounded, compacted grains, with average size $l_g \approx 100$ nm [Fig. 1(a)]. X-Ray diffraction measurements reveal a polycrystalline structure with crystallites in a wide spectrum of orientations [Suppl. Inf. 1]. At longer times, the (111) growth orientation dominates, giving rise to grains ($l_g \approx 300$ nm) with approximately pyramidal shapes. [Fig. 1(b)]. Interesting, the asymptotic pyramidal morphology resembles the typical KPZ-CdTe patterns observed during the growth of CdTe on Si(001) substrates^{19,21}. One-dimensional profiles of these two distinct regimes [Fig. 1(c)] give additional support for the description above, where a profile for the initially rough Kapton substrate (which has width $w_0 \approx 6$ nm, and correlation length $\xi_0 \approx 0.3\ \mu\text{m}$) is also shown.

Surface width $w(L, t)$, defined as the standard deviation of the height field, also exhibits different temporal regimes [Fig. 1(d)]. For very short times $t \in [7.5, 25]$ min, w decreases from $28(3)$ nm to $14(2)$ nm - numbers into parenthesis represent uncertainties in the last digits. This time interval is related to an interface smoothing mechanism, which will be explained below. Within the interval [25, 300] min the width does not grow, so that applying the usual $w \sim t^\beta$ scaling³⁰ we find $\beta_I = -0.01(7)$, where β is the growth exponent. This small exponent can also be interpreted as a logarithmic behavior of the roughness [$w(t) \sim \sqrt{\ln(t)}$], a fingerprint of EW class in 2D²². Finally, for $t \gtrsim 300$ min, usual power-law scaling arises with $\beta_{II} = 0.24(7)$. Such value provides an evidence of KPZ scaling (Table 1), although it also encompasses (within the error bar) the exponents for the linear ($\beta_I = 0.25$) and nonlinear ($\beta_n = 0.20$) molecular beam epitaxy classes²². Defining β_{eff} as the slope of five consecutive points in the $\log w \times \log t$ plot [Fig. 1d], we find compelling evidence that β_{eff} takes two distinct values separated by a characteristic time $t_c \approx 300$ min [inset of Fig. 1(d)]. Namely, one has $\beta_{\text{eff}} \approx 0$ for $t < t_c$ (the smoothing regime is not considered) and $\beta_{\text{eff}} \approx 0.24$ otherwise.

Now we turn to characteristic length scales, which are investigated by the (equal-time) height difference correlation function $C_h \equiv \langle [h(\mathbf{x} + \mathbf{l}, t) - h(\mathbf{x}, t)]^2 \rangle$. Brackets represent averages over different AFM images and positions \mathbf{x} , and l varies in the interval $[0, L]$. Accounting for the grains at surface (with average lateral size l_g), $C_h(l)$ is expected to scale as³¹:

$$C_h(l) \sim \begin{cases} l^{2\phi} & \text{for } l \ll l_g, \\ l^{2\alpha} & \text{for } l_g \ll l \ll \xi, \\ \text{const.} & \text{for } \xi \ll l, \end{cases} \quad (2)$$

where ϕ is a nonuniversal exponent related to the grain shape³¹ and α is the (universal) roughness exponent³⁰. Figure 1(e) shows $C_h(l)$ calculated for CdTe surfaces at different times. For $t \lesssim 720$ min, solely the scaling for $l \ll l_g$

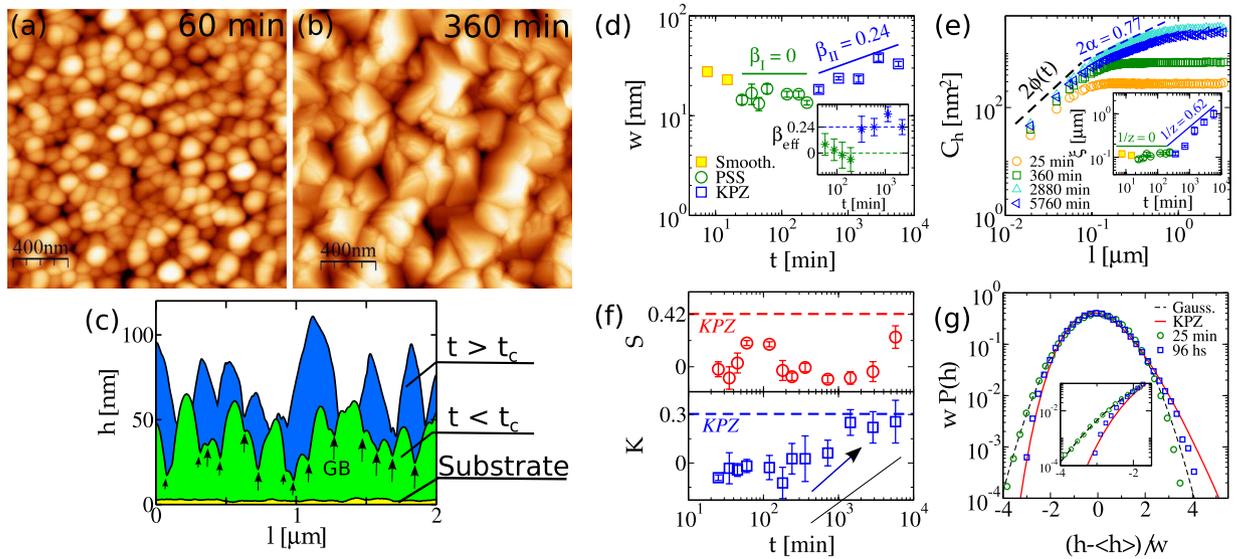


Figure 1. AFM images of CdTe surfaces for films grown at (a) 60 min (PSS regime) and (b) 360 min (beginning of the KPZ scaling). Typical 1D profiles are sketched out in (c). Black arrows indicate grain boundary (GB) sites considered in MC simulations. (d) Global CdTe surface width (w) as function of t . Different colored symbols and solid lines indicate different regimes. Inset shows the effective β exponent in time. (e) Height difference correlation function (C_h) versus l for different deposition times. Dashed lines are guides to eyes with slopes 1.2 and 0.77 (KPZ)¹³. Inset shows the temporal variation of the correlation length ξ . (f) Temporal evolutions of HDs' skewness (S) and kurtosis (K). The dashed lines indicate the universal KPZ values. (g) Rescaled HDs (with null mean and unity variance) for CdTe films (symbols), compared with Gaussian (dashed) and KPZ (solid line) HDs. Inset shows the same data highlighting the left tails.

	$t < t_c$	$t \gg t_c$	KPZ models
α	not determined	0.37(4)	0.3869(4) ⁵³
β	-0.01(7)	0.24(7)	0.241(1) ⁵⁴
$1/z$	-0.04(3)	≈ 0.63	0.623(3) ^{53,54}
$\alpha + z$	not determined	≈ 1.96	2^1
$S - [P(h)]$	0.03(6)	0.24(9)	0.42(1) ^{13,14}
$K - [P(h)]$	-0.06(8)	0.3(1)	0.34(1) ^{13,14}

Table 1. Scaling exponents (α , β and $1/z$) and HDs' cumulant ratios (S and K) for CdTe/Kapton surfaces at short (2nd) and long (3rd column) deposition times. The rightmost column shows the best known estimates for those quantities obtained from numerical simulations of 2D-KPZ models. For $t < t_c$, the experimental values of S and K are averages, while the ones for $t \gg t_c$ are those for the longest times investigated.

is observed, from which one obtains a time-dependent exponent $\phi(t) \in [0.6, 0.8]$. At longer times, the correlation length turns out to be larger than l_g , so that from the second scaling regime we measure $\alpha = 0.37(4)$ - in striking agreement with the best known estimate for the 2D-KPZ class [Table 1]. We remind that roughness exponents for EW, linear and nonlinear molecular beam epitaxy classes are, respectively, $\alpha_{EW} = 0$, $\alpha_l = 1$ and $\alpha_n = 2/3$. Hence, $\alpha = 0.37(4)$ is our first strong evidence of KPZ scaling. As an aside, we point out that a clear scaling regime $l_g \ll l \ll \xi$ has not been observed for CdTe/Si(100) system^{19,21}, possibly due to the short growth times analyzed there, as is also the case of the samples grown up to 720 min here. This is one of the reasons why a consistent universal α exponent is rarely observed in real grained surfaces.

At the beginning of the growth process, the correlation length is arguably of the same order of grains' size $\xi \simeq l_g$. Thence, the single crossover in C_h curves provides an estimate for ξ . For long times, ξ is associated with the second crossover. The insertion in Fig. 1(e) shows the evolution of ξ , from where one sees that during the interval in which the width does not grow, $t \in [25 \text{ min}, t_c]$, correlations also *do not*. Interesting, these properties are presented by finite-size interfaces at their steady states, where both w and ξ remain constant in time. Indeed, by assuming a power-law scaling like $\xi \sim t^{1/z}$, we find $1/z = -0.04(3)$ for $t < t_c$. On the other hand, in the asymptotic regime $t \gg t_c$ correlations start spreading through the system with a characteristic exponent $1/z \approx 0.63$, in the same way as stochastic models belonging to the KPZ class do [Table 1]. Similar results (not shown) are obtained by estimating ξ from the first zeros (or first minima) of the slope-slope correlation function, as done, e. g., in refs 19, 21.

These results demonstrate that the first regime is a *pseudo*-steady state (PSS), not described by the EW equation, for which $1/z = 0.5$ is expected²², while $1/z \approx 0$ is found here. On the other hand, the asymptotic regime is KPZ, as strongly suggested by the three independently measured exponents α , β and $1/z$. In addition, the Galilean invariance relation $\alpha + z = 2$ ¹ is quite well satisfied, with $\alpha + z \approx 1.96$. Table 1 summarizes the exponents obtained for each regime at side with the best known numerical estimates for 2D-KPZ class.

Last, we point that for $t < t_c$ height distributions (HDs) are Gaussian, while for $t \gg t_c$ they reasonably agree with the universal KPZ HD. Figure 1(f) shows temporal evolutions of the skewness $S \equiv \langle h^3 \rangle_c / \langle h^2 \rangle_c^{3/2}$ and kurtosis $K \equiv \langle h^4 \rangle_c / \langle h^2 \rangle_c^2$ (here $\langle X^n \rangle_c$ denotes the n^{th} cumulant of a random variable X). Within the PSS regime, one sees that $S \approx 0$ and $K \approx 0$. A clear crossover is observed in K , which approaches to the KPZ value $K_{KPZ} \approx 0.34$ ^{13,14} at long times. The skewness, on the other hand, seems to start converging latter and is still smaller than the KPZ one even for the longest time analyzed [Table 1]. Unfortunately, with the few data points available in the convergence region, we are not able to extrapolate S . Anyhow, Fig. 1(g) gives additional evidence of a Gaussian-to-KPZ crossover in the rescaled HDs, $P(h)$, as seen by the good collapse between the respective distributions in each regime. The agreement with KPZ HD is particularly clear in the left tails [inset of Fig. 1(g)] and at the peaks. Some deviations, however, are observed in the right tail, due to the skewness a bit smaller than the *asymptotic* KPZ one.

Modeling. In order to better comprehend the origins of the distinct regimes in the roughness scaling, relevant microscopic ingredients of the CdTe growth shall be clarified. At the very beginning of the deposition process, one observes that the roughness fast increases from $w_0 \approx 6 \text{ nm}$ (Kapton substrate) to $w = 28(3) \text{ nm}$ (for $t = 7.5 \text{ min}$), as inferred from Fig. 1(d). First, deposition temperature is relatively low ($T = 150^\circ\text{C}$), so that diffusion of adsorbed species is slow, leading to the nucleation of a large number of CdTe islands at the submonolayer regime. Second, it seems to exist a strong aversion of CdTe molecules into wetting the Kapton surface, inducing the formation of 3D islands (grains), according to the Volmer-Weber growth mode. Thereby, islands with small lateral sizes (l_g) and large heights (h_g) are initially formed, which may explain the fast w increasing.

To understand the subsequent smoothening (the decreasing w) and PSS regimes, the key points are: (i) CdTe layers have been observed to develop a strong texture in the (111) direction^{19,21}, implying that (111)-grains grow faster than the ones with other crystallographic orientations; and (ii) the amorphous nature of the Kapton substrate leads to the formation of CdTe grains in a wide spectrum of crystallographic orientations, so that (111)-grains shall take a long time to dominate the surface. This is in contrast with the situation on (crystalline) Si substrates, where a majority of (111)-grains is observed since short times [Suppl. Inf. 1]. Keeping these informations in mind, CdTe/Kapton roughness scaling can be explained as follows. When initial grains collide, forming a film that completely covers the substrate, some large height differences at surface obviously disappear, leading to the fast smoothening observed for $t \in [7.5, 25] \text{ min}$. In the subsequent multilayer regime, we may expect that the CdTe growth dynamics proceed as explained in ref. 21: defect sites at and around the grain boundaries (GBs) between two or more (collided) grains inhibit mass transport of adsorbed species between them, preventing the spreading of correlations on the surface. For instance, in CdTe/Si(100) system (deposited at $T = 150^\circ\text{C}$) such condition led to a Random Deposition growth (for which $\beta = 1/2$ and $1/z = 0$) at short times²¹, with grain peaks evolving in an uncorrelated way. For the present system, one could expect a similar behavior, and indeed we find $1/z \approx 0$ for $t < t_c$. However, there exists a key distinction here. Because of the fact in (ii), grains with large height [mostly the (111) ones] are considerably surrounded by smaller [mostly non-(111)] ones up to relatively long times. When the low height [non-(111)] grains are covered up by higher (111) ones, allowing these ones to collide, a smoothening mechanism similar to that of the very initial growth times happens. In short, while deposition tends to yield an increasing roughness, collisions of (111) grains after covering other ones lead to a smoothening. Very interesting, during a long time interval ($t \in [25, 300] \text{ min}$) both mechanisms compensate each other, so that w (and ξ) remains constant, giving rise to the PSS regime. It is worthy mentioning that the smoothening operative here - driven by grain collisions - is quite different from that studied in stochastic growth models deposited on rough substrates³².

At very long growth times, surface becomes dominated by (111) crystallites - the probability of finding a (111) grain in the film becomes $\geq 90\%$ [Suppl. Inf. 1] -, so that the smoothening effect becomes negligible. Relaxation of defects at GBs eventually occurs and coalescences and spreading of correlations turn out to be the relevant mechanisms for the subsequent dynamics. Coalescence/packing of (111) grains is already known to yield a velocity excess in CdTe growth, leading to the KPZ scaling^{19,21}.

The reasoning above is corroborated by a discrete 1D model, proposed in ref. 21 to explain the short-time coalescence dynamics of CdTe/Si(001) films. Since our aim here is to demonstrate the role of a large initial roughness and GB defects to yield the PSS regime, we use (1D) height profiles extracted from (2D) CdTe images (at $t = 60 \text{ min}$) as the initial condition. Moreover, to mimic the experimental situation, where the CdTe lattice constant is $\sim 1 \text{ nm}$, we assume the same for the simulations and rescale the profiles accordingly (e. g., a profile of $2 \mu\text{m}$ shall correspond to $L \sim 2000$ sites, which is obtained by enlarging the original 512 pixel profile by a factor 4). For special sites, mimicking the grain boundaries (GBs), an energy barrier $E_{GB} = 0.10 \text{ eV}$ is locally assigned, in order to hamper diffusion of particles towards that region [for sake of simplicity we set GB sites at the local minima at the profiles - see Fig. 1(c)]. It is assumed that diffusion and aggregation occur much faster than adsorption (desorption is not considered), so that each particle permanently aggregates before the arrival of the next one at surface. Thus, for each event of deposition, the following rule holds: a particle, randomly deposited on the surface, diffuses until finding a site i satisfying the restricted solid-on-solid condition $|h_i - h_{i+1}| < 1$ (h_i is the height of site i , measured from the substrate), where it permanently aggregates. Diffusion towards a GB site occurs with probability $P_d = e^{-E_{GB}/k_B T}$, where k_B is the Boltzmann constant, while diffusion to regular sites occurs with unity probability ($P_d = 1$). Relaxation of defects around GBs is activated through deposition and rearrangement of particles. Then, in the model, whenever a particle is deposited at a given GB site, it might become a regular site with

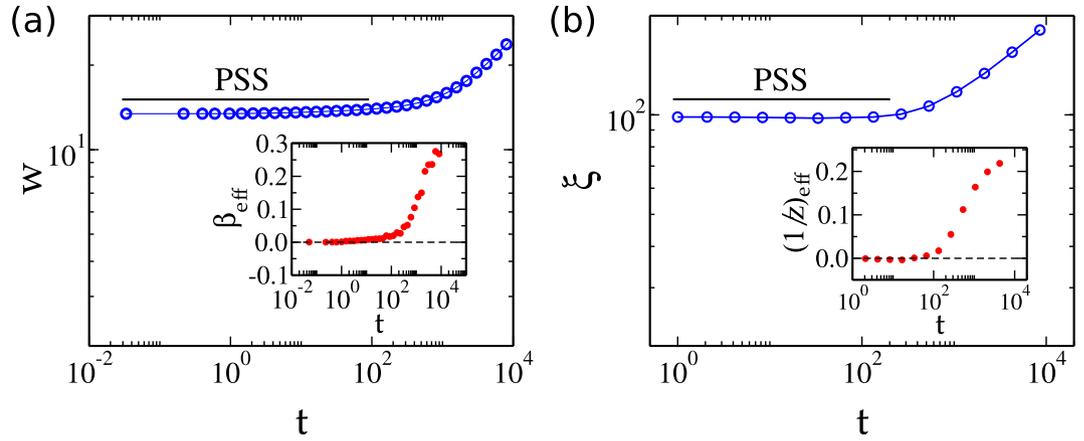


Figure 2. Temporal evolutions of (a) interface width w and (b) correlation length ξ for the 1D model. Insertions show the effective (a) growth β_{eff} and (b) inverse dynamic $1/z_{\text{eff}}$ exponents as functions of time.

CdTe- γ_n	KPZ- γ_n	CdTe- $[P(w_2)]$	KPZ- $[P(w_2)]$	CdTe- $[P(m)]$	KPZ- $[P(m)]$
$\gamma_1 = 0.57(12)$	0.4830(30)	$R = 1.87(8)$	2.05(5)	$R = 7.3(5)$	7.3(4)
$\gamma_2 = 1.96(29)$	2.214(15)	$S = 2.1(3)$	2.04(4)	$S = 0.83(9)$	0.84(2)
$\gamma_3 = 3.60(52)$	3.946(27)	$K = 7.6(2.4)$	7.3(3)	$K = 1.19(34)$	1.14(5)

Table 2. (Left) Asymptotic γ_n exponents from generalized FV scaling relation 3. The KPZ values were calculated using the estimates of α and β in^{53,54}. Cumulant ratios R , S and K for stationary width (middle) and maximal height (right) distributions calculated with WBCs. All KPZ values for the cumulants were extracted from ref. 33.

probability $P_R = e^{-E_R/k_B T}$, where we set $E_R = 0.30$ eV. The time scale (“min”) is defined so that the deposition rate is given by 14 ML/“min”, similarly to the experiment.

A clear regime of constant roughness is observed at initial times of the growth model, being replaced by a scaling regime at longer times [Fig. 2(a)]. The effective growth exponents confirm both behaviors, since $\beta_{\text{eff}} \approx 0$ is found for $t < t_c$ and $\beta_{\text{eff}} \neq 0$ for $t \gg t_c$ [inset of Fig. 2(a)]. Coincidentally, there exist even quantitative agreement between both w (≈ 13 at short times) and t_c (≈ 300 “min”), with the experiment: $w \approx 15$ nm (in PSS regime) and $t_c \approx 300$ min [Fig. 1(d)]. The correlation length parallel to substrate (ξ) is shown in Fig. 2(b) as a function of time, with the respective effective (inverse) dynamic exponents ($1/z_{\text{eff}}$) displayed in the insertion. The almost constant ξ at short times ($t < t_c$), yielding $1/z_{\text{eff}} \approx 0$, confirms the existence of a PSS regime in the model. This strongly suggests that the interplay of defects at GBs (inhibiting intergrain diffusion and grain coalescence, as well as the spreading of correlations at surface) and an initial condition with grains of very different heights may be the origin of the PSS in CdTe/Kapton, as explained above.

Despite the success of this model for explaining the short-time behavior of CdTe growth, as also observed in ref. 21, we stress that *no* agreement with experiments is expected for $t \gg t_c$, since the model clearly does not have an asymptotic scaling in KPZ class. Moreover, it is 1D and cannot explain the asymptotic dynamics of a 2D system. For this matter, a much more complex off-lattice model is required taking into account the existence of grains with different orientations and growth velocities, as well as the effect of grain packing and so on.

Generalized Family-Vicsek scaling and log-normal distributions. From this section we explore CdTe surfaces as an experimental testbed for additional scaling and distributions theoretically predicted for the KPZ class and, conversely, obtain further confirmation of the results presented so far. Let us start with a recent generalization³³ of the Family-Vicsek (FV)³⁰ scaling *ansatz*, which has not been verified experimentally yet. According to ref. 33, the squared local width, $w_2(l, t)$ - calculated in square windows of lateral size $l \ll L$ that span the whole surface - is a fluctuating variable whose n^{th} cumulant of its distribution $[P(w_2)]$ behaves as:

$$\langle (w_2)^n \rangle_c = l^{2n\alpha_f} (t/l^z), \tag{3}$$

where $f_n(u) \sim u^\gamma$ for $u \ll 1$, and $f_n(u) \sim \text{const}$ for $u \gg 1$. The γ_n exponents are given by $\gamma_n = 2n\beta + [(n-1)d_s]/z$, and their values for 2D-KPZ class, calculated from the best known estimates of β and z , are summarized in Table 2. Note that for $n = 1$, the classical FV scaling is recovered.

Bearing in mind that γ_n exponents are related to the regime for which $\xi \ll l$, and relied upon our estimate for ξ made in Fig. 1(e), we conclude that a suitable interval for performing experimental measurements is $l \in [20, 160]a$, with $a \equiv 10 \mu\text{m}/512$ being the pixel size. The upper limit ($160a \ll L$) is chosen to guarantee good statistics. Figure 3(a,b) display, respectively, the variation of the second and third cumulants of $P(w_2)$ in time. The initial almost constant behaviors observed, consistent with $\beta \approx 0$ and $1/z \approx 0$, give further evidence of the existence of a

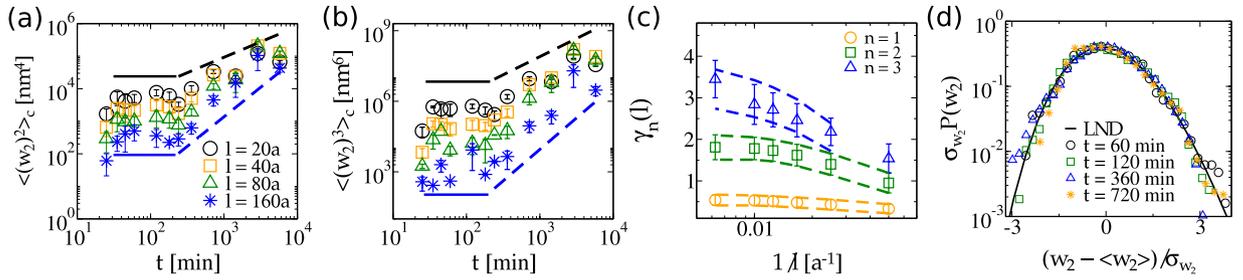


Figure 3. Temporal evolution of the second (a) and third (b) cumulants of width distributions, $P(w_2)$, calculated for windows of different lateral sizes l . Solid and dashed lines are guide to eyes indicating the PSS and KPZ regime, respectively. Top (black) and bottom (blue) dashed lines have the slope of the curves for $l = 20a$ and $l = 160a$, respectively. (c) Exponents $\gamma_n(l)$ as a function of $1/l$. (d) Rescaled width distributions for CdTe surfaces (symbols), at several growth times and calculated for $l = 80a$, along with the LND (solid line). Here, $\sigma_{w_2} \equiv \sqrt{\langle (w_2)^2 \rangle_c}$.

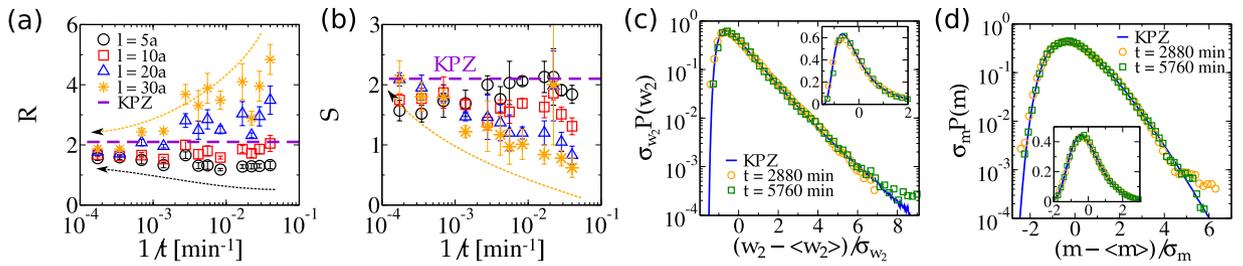


Figure 4. (a) Inverse of the variance coefficient R and (b) skewness S as function of $1/t$ for (stationary) width distributions, for several window sizes l . Rescaled (c) width $[P(w_2)]$ and (d) maximal height $[P(m)]$ distributions, for CdTe (symbols) and 2D-KPZ models (solid blue lines). Insets show the same data in log-linear scale. Here, $\sigma_X \equiv \sqrt{\langle X^2 \rangle_c}$ is the standard deviation of $X = w_2, m$.

PSS regime. Algebraic scaling arise at long times, from which the exponents shown in Fig. 3(c) are measured. Hydrodynamic limit demands finding γ_n after taking the limits $l (\leq L) \rightarrow \infty$ and $t \rightarrow \infty$. Since the last requirement is not of easy experimental implementation, we analyze *effective* γ_n 's for different l s and extrapolate them to $l \rightarrow \infty$, as done in Fig. 3(c). Exponents obtained from such procedure are summarized in Table 2, with all values consistently in agreement, within the error bars, with those expected for the KPZ class.

A more complete characterization of w_2 fluctuations is set down by the (full) width distributions, $P(w_2)$. For a given surface, as the window size l approaches to L , with $\xi \ll l$, $P(w_2)$ approaches to a Dirac delta function (because the number of windows converge to unity). More interesting, however, is that $P(w_2)$ converges first to a log-normal distribution (LND) before reaching the delta. As explained in ref. 33, the emergence of LNDs is a general feature of low-correlated growth (when $\xi \ll l$) that does not depend on the universality class. We experimentally test this conjecture by comparing rescaled (to zero mean and unity variance) $P(w_2)$ for CdTe interfaces, for large l and small t , with the LND [Fig. 3(d)]. Experimental distributions collapses nicely onto LND at their peaks and tails, for *both* PSS and KPZ regimes, confirming the role of LND in surface growth context. A more detailed analysis of this subject is presented in Suppl. Inf. 2.

Stationary fluctuations. While width fluctuations for $\xi \ll l \ll L$ are given by log-normal distributions regardless the universality class of the system, in the stationary limit $\xi \gg l$ different and universal pdf's, $P(w_2)$, are expected for each universality class. Width distributions for the stationary regime were analytically calculated in the 90's for 1D linear growth models^{34,35} assuming periodic boundary conditions (PBC). Subsequent work³⁶ called attention for the importance of considering window boundary conditions (WBC), which parallels the experimental way of obtaining $P(w_2)$. More challenging, the 2D distributions for WBC have been numerically investigated^{20,33,37,38}, and experimentally used to confirm the universality of CdTe/Si(001)^{19,21}, oligomer²⁰ and oxide³⁸ growing films. The successful agreement between numerical and experimental width distributions in 2D motivated their analysis also in 1D KPZ interfaces of nematic liquid-crystal system⁷. The systematic study of these distributions³³ showed that the best way to verify their asymptotic universality is performing successive extrapolations of their cumulant ratios for $t \rightarrow \infty$ and then for $l \rightarrow \infty$. Although we are not able to implement this procedure here, due to statistical fluctuations in the data [Fig. 4], we find that for large t and l the cumulant ratios tend to approximate to the KPZ ones. A relaxed methodology relies upon guaranteeing that cumulant ratios converge to *plateaus regions* at sufficiently long times, with $l \lesssim 0.3\xi$ being a safe limit over which experimentalists should prop up³⁷.

For CdTe surfaces, one has $\xi \gtrsim 90a$ for $t \geq 2880$ min, hence $l \leq 30a$ is considered in our analyses. In Fig. 4(a), the ratio $R \equiv \langle w_2 \rangle_c / \langle (w_2)^2 \rangle_c^{1/2}$ (the inverse of the coefficient of variance) is plotted as function of $1/t$ for several l 's. Indeed, at large t and l , experimental data systematically approach to the R value expected for the 2D-KPZ class. Analogous behavior is observed for S [Fig. 4(b)] and K ratios [Suppl. Inf. 2]. The values for $t = 5760$ min and $l = 30a$, the closest ones to the asymptotics, present a remarkable agreement with the universal KPZ ratios [see Table 2]. Further confirmation of such agreement is provided by the collapse of rescaled width distributions for CdTe surfaces onto the universal KPZ curve at both tails and at the peak [Fig. 4(c)].

A quite similar calculation can be made for evaluating the stationary distributions, $P(m)$, of local extreme heights m , where $m = h^* - \langle h \rangle$, and h^* is either the maximal or minimal value of h inside a window of size $l \ll \xi$. Extreme statistics plays a relevant role in several areas of knowledge and are usually related to catastrophic events (see, e.g., ref. 39 for a recent review). The scaling of the global m and its distribution have been investigated in a number of works^{40–44}, while the universality of the local distribution [$P(m)$, with WBC] has been numerically demonstrated more recently in several numerical and experimental studies^{7, 19–21, 33, 38}. Following the same recipe used for calculating $P(w_2)$, we determine $P(m)$ (for maximal heights) and its related cumulant ratios (R, S, K), whose convergence with t and l is presented in Suppl. Inf. 2. Their asymptotic values, displayed in Table 2, are in striking agreement with the KPZ ones. A nice collapse of rescaled distributions $P(m)$ for CdTe surfaces onto the KPZ curve is observed around three orders of magnitude from the peak [Fig. 4(d)]. Altogether, these results for stationary distributions give a quite compelling confirmation of KPZ universality in the growth of CdTe films on Kapton substrates.

KPZ ansatz and spatial covariance. The asymptotic evolution of the (1-point) height of a growing KPZ interface can be summarized in the expression⁴⁵:

$$h(t) \simeq v_\infty t + s_\lambda (\theta t)^\beta \chi, \quad (4)$$

where v_∞ (the asymptotic growth velocity), s_λ (the signal of λ), and $\theta \equiv (A^{1/\alpha} \lambda)$ are system-dependent parameters. χ is a random variable distributed according to universal (height) distributions $P(\chi)$, which depend on the substrate dimension⁷ and initial conditions⁴. The so-called “KPZ ansatz” (eq. 4) can also describe the dynamics of growing interfaces belonging to other universality classes, provided that θ is suitably redefined¹².

Following the procedure introduced in ref. 20, we may estimate θ, A and λ for the CdTe/Kapton surfaces by using the (2-point) spatial covariance C_s , defined as:

$$C_s(l, t) = \langle [h(\mathbf{x} + \mathbf{l}, t)h(\mathbf{x}, t)] \rangle - \langle h \rangle^2 \simeq (\theta t)^{2\beta} g \left[\frac{A_h l^{2\alpha} / (\theta t)^{2\beta}}{2} \right], \quad (5)$$

where $g(u)$ is an universal scaling function, and A_h is the amplitude associated to the height difference correlation function C_h (eq. 2), i.e. $C_h(l) = A_h l^{2\alpha}$ over the $l_g \ll l \ll \xi$ scale. Functions $g(u)$ are analytically known for different initial conditions in 1D¹¹, and have been experimentally confirmed in turbulent growth of nematic liquid-crystal phases⁶. Universal scaling functions also exist in 2D, as observed numerically^{15, 20} and confirmed in the growth of oligomer films²⁰.

Noting that $C_s(0, t) = \langle h^2 \rangle_c$, from eq. 4 one has that $g(0) = C_s(0, t) / (\theta t)^{2\beta} = \langle \chi^2 \rangle_c$. The universal value of $\langle \chi^2 \rangle_c$ is numerically known to be $\langle \chi^2 \rangle_c \simeq 0.24$ ^{13, 15}, for 2D-KPZ interfaces with flat IC. We estimate the experimental value of θ by assuming the universality of $\langle \chi^2 \rangle_c$ in $\theta \simeq [\langle h^2 \rangle_c / \langle \chi^2 \rangle_c]^{1/2\beta} / t$, and using our estimates for $\langle h^2 \rangle_c = w^2$ from Fig. 1(d). We obtain $\theta \approx 24 \times 10^3$ [$nm^{1/\beta}$]/[min] for $t = 2880$ min and $\theta \approx 7 \times 10^3$ [$nm^{1/\beta}$]/[min] for $t = 5760$ min. The different values are expected due to statistical fluctuations in w [Fig. 1(d)].

Now, considering the obtained values for θ , we find A_h by making the rescaled $C_s(l, t)$ curves to collapse onto the KPZ universal scaling function $g(u)$ [Fig. 5(a)]. Such procedure yields $A_h \approx 5000$ [$nm^2/\mu m^{2\alpha}$] for $t = 2880$ min and $A_h \approx 4400$ [$nm^2/\mu m^{2\alpha}$] for $t = 5760$ min. On the other hand, from the definition of A_h , we also estimate its value from the (expected) plateaus in the $C_h(l)/l^{2\alpha} \times l$ curves, as done in Fig. 5(b). Data for $t = 2880$ min has a clear plateau at $A_h \approx 4400$, which is quite close to the value estimated from the collapse of C_s . For $t = 5760$ min, however, the plateau is absent due to an effective α exponent a bit smaller than the KPZ value in the $C_h \times l$ scaling [Fig. 1(e)].

Finally, knowing θ and A_h , we determine the experimental value of λ - the key KPZ parameter. Using the relation $A_h/A \approx 0.6460$ ²⁰ and the A_h from the collapses, we obtain $A \approx 7740$ [$nm^2/\mu m^{2\alpha}$] for $t = 2880$ min and $A \approx 6656$ [$nm^2/\mu m^{2\alpha}$] for $t = 5760$ min. Re-inserting these values into the definition of θ , we find $\lambda \approx 3.6 \times 10^{-2}$ nm/s and $\lambda \approx 1.5 \times 10^{-2}$ nm/s, respectively, for $t = 2880$ min and $t = 5760$ min. These values are rather small when compared to that reported for oligomer films ($\lambda \approx 5$ nm/s)²⁰, but they are consistent with the CdTe growth rate $F \approx 23 \times 10^{-2}$ nm/s. Moreover, a small λ is consistent with the very slow PSS-KPZ crossover found here. This may also explain the initial uncorrelated growth observed in CdTe/Si(100)²¹ for $T = 150^\circ\text{C}$, which possibly gives place to KPZ scaling at longer times. We remark that at higher temperatures, larger values of $|\lambda|$ are expected, as discussed in ref. 21.

It is noteworthy the good data collapse between covariances for CdTe surfaces and 2D-KPZ models [Fig. 5(a)]. This collapse provides additional evidence of an universal 2D-KPZ spatial covariance and, at the same time, gives a final confirmation that CdTe/Kapton films evolves asymptotically according to the KPZ class.

Summary and final Discussion

We have analyzed the kinetic roughening of CdTe films deposited on Kapton substrates at relatively low temperature and intermediate deposition rate. The rough and non-crystalline (polymeric) substrate allows, at the

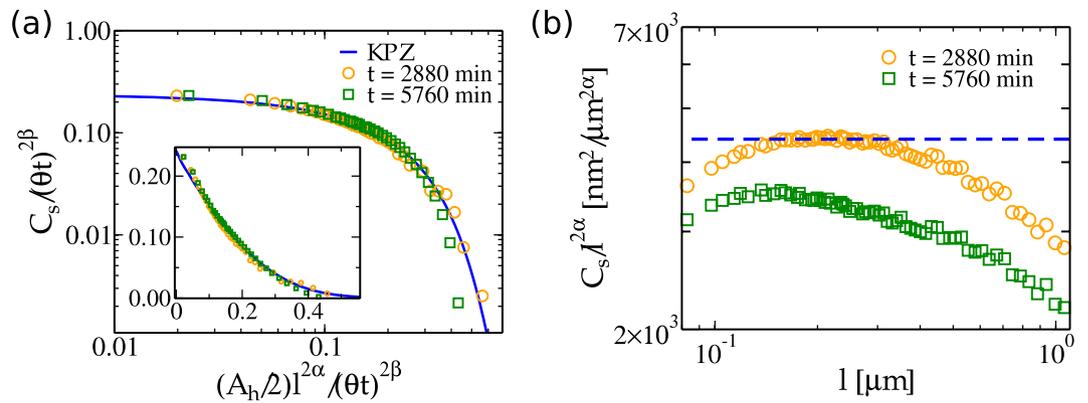


Figure 5. (a) Rescaled spatial covariance for KPZ class¹⁵ (solid line) compared with the ones for CdTe surfaces (symbols). Inset shows the same data in linear scale. (b) Rescaled height difference correlation function $C_h l^{2\alpha}$ versus l for CdTe surfaces at long times. The dashed line indicates the estimate of A_h for $t = 2880$ min. Rescaling was performed using $\alpha = 0.3869$ ⁵³ and $\beta = 0.241$ ⁵⁴.

submonolayer regime, the formation of small 3D-CdTe grains with several crystallographic orientations and large height differences, yielding a large global roughness at very initial growth times. Smoothing and a long pseudo-steady state (PSS) regime take place in the sequence, as a consequence of grain collisions, with the former occurring at the transition between the submonolayer and multilayer growth. In the PSS regime, the smoothing comes from the collisions of high [mostly (111)] grains after covering up smaller [mostly non-(111)] ones. Interesting, in such regime roughening and smoothing are counter balanced, so that interface width and correlation length ξ do not grow, exactly as they would do in a genuine steady state of finite-size systems. The reasoning of a combined surface roughening and smoothing leading to a PSS is supported by simulations of a 1D phenomenological model, which captures main features of grain coalescence in CdTe growth. On the other hand, the asymptotic CdTe growth regime is shown to belong to the KPZ class by (i) several (independently measured) scaling exponents, in addition to universal (ii) height, (iii) local square-width and (iv) extreme height distributions. Final striking evidence of KPZ scaling is given by (v) the spatial covariance, which allowed us to estimate the KPZ “excess velocity” of the studied films as $\lambda \sim 10^{-2}$ nm/s. Overall, these results support that high vacuum vapor deposition of polycrystalline CdTe is a standard system belonging to KPZ class, regardless the substrate nature. This might stimulate previous works on CdTe grown on glass^{46,47} to be revisited considering longer deposition times. Of course, for CdTe deposited under other growth conditions, e.g. by sputtering⁴⁸, where inhomogeneous flux of particles and shadow effects can play a role, KPZ scaling may not take place.

For width fluctuations in the limit of low correlations ($\xi \ll l$), we have experimentally demonstrated the emergence of log-normal distributions, in both PSS and KPZ regimes, confirming recent conjectures³³. Moreover, from the temporal scaling of their cumulants, we found scaling exponents in good agreement with the KPZ ones - also in agreement with those obtained by the standard width and spatial correlation function. This fact demonstrates that the generalized Family-Vicsek scaling³³ is a useful tool even for estimating exponents from experiments.

We remark that the PSS regime could be easily misunderstood as an Edwards-Wilkinson growth, since both are characterized by vanishing β and Gaussian height distributions. This shows the necessity of measuring as many quantities as possible to confirm the class of real growing systems, specially not relying only upon the exponents. Note that we had to grow films up to $t = 5760$ min (4 days!) in order to observe the KPZ scaling regime only one decade in time (in $w \times t$ plot). Similar difficulty was already observed in previous KPZ systems¹⁸. The presence of grainy morphology also severely hampers the calculation of the exponent α . A consequence of using only the exponents from the traditional Family-Vicsek scaling, usually estimated from short deposition times, is the large number of existing works reporting scaling analyses of real interfaces without association to any universality class.

We also point that an initial PSS regime might be rather general, since it was also observed in organosilicone films deposited by chemical vapor deposition at atmospheric pressure on polymeric substrates^{49,50} and in plasma etched polymeric films⁵¹. Even though the microscopic origin of this behavior seems quite different in such systems, it is somewhat intriguing that all these evidences of the PSS are associated with polymeric substrates.

Finally, the KPZ mechanism in CdTe films comes from the packing of grains, which yields a velocity excess in the growth, as explained in refs 19, 21. Obviously, results presented here do not have any relation with a possible artificial KPZ scaling induced by AFM tip effects⁵². Note that typical tip radius (r) is $r \approx 10\text{--}20$ nm, corresponding to the size of our image pixel ($a \approx 19.5$ nm), while the average CdTe grain size is $l_g \approx 0.7$ μm in the asymptotic KPZ regime. Namely, l_g is at least 35 times larger than r and, in such situation, possible effects of the AFM tip are negligible. More important, even when CdTe grains are smaller and some AFM tip effect could be expected, KPZ scaling is not found neither here (at short times) nor elsewhere^{46,47}.

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Acknowledgements

RALA thanks fruitful discussions with I. S. S. Carrasco, F. A. A. Reis and T. Sasamoto, and a careful reading of preliminary versions of the paper by I. S. S. Carrasco and K. A. Takeuchi. Authors acknowledge support from Brazilian funding agencies CAPES, FAPEMIG and CNPq. RALA acknowledge financial support by KAKENHI from JSPS - No. 16J06923.

Author Contributions

R.A.L.A. grew samples, performed AFM measurements, built computational algorithms for data analyzes and wrote the paper. S.O.F. designed, managed the whole experiment and analyzed the results. I. Ferraz also grew films and contributed with AFM and XRD measurements. T.J.O. analyzed the results, performed simulations and wrote the paper. All authors reviewed the manuscript.

Additional Information

Supplementary information accompanies this paper at doi:[10.1038/s41598-017-03843-1](https://doi.org/10.1038/s41598-017-03843-1)

Competing Interests: The authors declare that they have no competing interests.

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